Dependable Systems

# Definitions and Metrics

Dr. Peter Tröger

Sources:

J.C. Laprie. Dependability: Basic Concepts and Terminology Eusgeld, Irene et al.: Dependability Metrics. 4909. Springer Publishing, 2008 Echtle, Klaus: Fehlertoleranzverfahren. Heidelberg, Germany : Springer Verlag, 1990. Pfister, Gregory F.: High Availability. In: In Search of Clusters., S. 379-452

- Umbrella term for operational requirements on a system
  - IFIP WG 10.4: "[..] the trustworthiness of a computing system which allows reliance to be justifiably placed on the service it delivers [..]"
  - IEC IEV: "dependability (is) the collective term used to describe the availability performance and its influencing factors : reliability performance, maintainability performance and maintenance support performance"
  - Laprie: "Trustworthiness of a computer system such that reliance can be placed on the service it delivers to the user "
- Adds a third dimension to system quality
- General question: How to deal with unexpected events ?
- In German: ,Verlässlichkeit' vs. ,Zuverlässigkeit'



# System Type Examples

#### • Dependable (reliable) system

• Delivers a required service during its lifetime

#### • Fault-tolerant computer system

• Continues correct service provisioning in the presence of faults

#### • Real-time computer system

• Deliver a service within given time constraints (physical time, duration, ...)

#### Responsive computer system

• Fault-tolerant real-time system

# System Integration Levels

- Dependability has to be considered at every level
- Decomposition approach influences dependability success

Java EE Application
Application Modules
Application Server
Virtual Runtime Environment
Operating System
Virtualization Environment
Operating System
Compute Blade
Blade Center
Integrated Circuits

#### Dependability Stakeholders

- System Entity with function, behavior, and structure
  - A number of components or subsystems, which interact under the control of a design [Robinson]
- Service System behavior abstraction, as perceived by the user
- User Human or physical system that interacts with the systems service
- Specification Definition of expected service and delivery conditions
  - On different levels, can lead to specification fault
- Reliance demands assessment of **non-functional dependability attributes**
- Provide ability for trustworthy service delivery by dependability means
- Undesired (maybe expected) circumstances form dependability threats

# Dependability Tree (Laprie)





# Dependability Threats

#### • System failure - ,Ausfall'

- Event that occurs when the service no longer complies with the specification / deviates from the correct service.
- System error ,Fehler(zustand)'
  - Part of system state that can lead to subsequent failure
  - Some sources define errors as active faults not in this course ...
- System fault ,Fehler(ursache)'
  - Adjudged or hypothesized cause of an error
- Failure occurs when error state alters the provided service
- Systems are build from connected components, which are again systems
- Fault is the consequence of a failure of some other system to deliver its service

### Chain of Dependability Threats (Avizienis)



# Faults

- High diversity in possible sources and types
  - Fault nature
    - Accidental faults (,Zufallsfehler') vs. intentional faults (,Absichtsfehler')
    - Intentional faults are created deliberately, presumably malevolently
  - Fault origin viewpoints (not exclusive)
    - Phenomenological causes: Physical / natural faults vs. human-made faults
    - System boundaries: **Internal** faults (part of system state that produces an error) vs. **external** faults (interference with the environment)
    - Phase of creation: **Design** faults vs. **operational** faults
  - Temporal persistence
    - Permanent faults vs. temporary faults

## Observations on Faults

- An external fault is a design fault inability or refusal to foresee all situations
- Design faults are created during system development, system modification, or operational procedure creation and establishment
- Just replacing broken version of the same component leads to recurrent faults
- Physical faults are accidental faults
- Temporary external accidental physical faults are also called transient faults
- Temporary internal accidental faults are also called intermittent faults
  - Examples: Pattern-sensitive memory hardware, system overload
  - Arbitrary concept Permanent faults with unknown activation condition
- Intentional and design faults are human-made faults, might be malicious faults
- Hardware production defects are typically physical faults

Dependable Systems Course

### Observations on Faults

- A fault is **active** when it produces an error
- A non-active internal fault is a dormant / passive fault (,inaktive Fehlerursache')
  - Origin in hardware fault analysis often cycling between dormant and active
- Many specialized versions of the term ,fault', e.g. bug
  - Heisenbug Intermittent software fault, Bohrbug Permanent software fault
  - Mandelbugs Appear chaotic due to many dependencies
- Fault-tolerant system design is a contradiction
  - Design demands specification, faults are non-specified cases
  - Solution: Specification for fault-free case + additional fault specification
- Fault can mean performance or timing faults (derivation from expected load / timing)

















# Fault Model

- Faults can be classified into different categories on different abstraction levels
  - Physics
  - Circuit level / switching circuit level
    - Interesting for hardware design research (not this course)
    - Investigate logical signals on connections
      - stuck-at-zero, stuck-at-one, bridging faults, stuck-open
  - Register transfer level
  - Processor-memory-switch (PMS) level
  - Hardware system level
  - ... (Software) ...

# Physical Faults [Goloubeva]

- Highly energized particles originate from space, atmospheric, or ground radiation
  - Cosmic radiation, solar heavy ions, solar protons, ...
- Interaction of particle that strikes a circuit atomic displacement, direct ionization, indirect ionization created by nuclear reactions
- Smaller structures are sensitive to ionization effects from all kinds of particles
- Single Event Upset (SEU) injected charge changes content of a memory bit
- Dynamic random access memory (DRAM) typical building blocks for main memory
  - No inherent refreshing, influence on storage capacitor changes value
- Static random access memory (SRAM), for caches, registers, pipeline, ...
  - Impact on restoring transistor leads to invalid refresh operation

## Physical Faults [Goloubeva]

- Logic circuits: Shrinking size, reduction of power supply, increase of frequency
  - Noise margin is extremely reduced, single-event strike impacts circuit lines
- Single Event Transient (SET): Particles modify voltage in a combinational circuit
  - Can be modeled at gate level as erroneous transition on the gate output



# Fault Model for Semiconductor Memories

- Stuck-at-1 or stuck-at-0 (hard) faults, transition / bit-flip faults (0->1, 1->0)
- Open and short circuits Too much or too little metallization; Also open bonds
- Input and output leakage Leakage current in excess of the specified limit
- Multiple writing Data written into more than one cell when writing into one cell
- Pattern sensitivity Device does not perform reliably with certain test pattern(s)
- Refresh dysfunction Data are lost during the specified minimum refresh time
- Write recovery Write followed by reading/writing at different location resulting in reading/writing at same location
- Sense amplifier recovery Data accessed for a number of cycles are the same and then suddenly changed, sense amplifier tends to stay in the same state
- Sleeping sickness Memory loses information in less than the stated hold time (typically tens of milliseconds)

# Fault Model for Semiconductor Memories

- Decoder malfunction Inability to address same portions of the array
  - No cell accessed by certain address, multiple cells accessed by certain address
  - Certain cell not accessed by any address
  - Certain cell accessed by multiple addresses
- Bridging fault Short between cells, AND type or OR type
- State coupling fault Coupled (victim) cell is forced to 0 or 1 if coupling (aggressor) cell is in given state
- Inversion coupling fault Transition in coupling cell inverts coupled cell
- Idempotent coupling fault Coupled cell is forced to 0 or 1 if coupling cell transits from 0 to 1 or 1 to 0
- **Disturb fault** Victim cell forced to 0 or 1 if we read or write aggressor cell (may be the same cell)

# System-Level Fault Model

- Idea from hardware background, meanwhile also in software
  - Usage: How many faults of different classes can occur ? What do I tolerate?
- Process as black box, only look on input and output messages
- Link faults are mapped to the participating components
- Timing of faults: Fault delay, repeat time, recovery time, reboot time, ...
- Every participating component would need a fault model pick the most urgent ones





# System-Level Fault Model [Cristian]

- Fail-Stop Fault : Processor stops all operations, notifies the other ones
- Crash Fault : Processor looses internal state or stops without notification
- Omission Fault : Processor will break a deadline or does not react to some task at all
  - Send / Receiver Omission Fault: Necessary message was not not sent / not received in time
- **Timing** Fault / **Performance** Fault : Processor stops / reacts to a task before its time window, after its time window, or never
- Incorrect Computation Fault : No correct output on correct input
- Byzantine Fault / Arbitrary Fault : Every possible fault
  - Authenticated Byzantine Fault : Every possible fault, but authenticated messages cannot be tampered

#### Errors

- State of the system, not an event !
- Escalates to failure depending on
  - Intentional / unintentional redundancy
  - System activity
  - User's definition of a failure
    - Examples: Maximum outage time, acceptable delay, retransmission rate
- System activity can overwrite the error state before damage is happening
- Latent (not recognized) vs. detected error coming from an active fault
- Hardware often contains unintentional redundancy, makes it difficult to test

### Hardware Error Models [Goloubeva]

- Hardware faults effect state information, e.g. register values
  - Stuck-at and other hardware faults therefore can also be denoted as error
- More interesting to investigate resulting effects on system-level
  - Single data error Program data is corrupted (in cache, memory, or register)
  - Single code error Effect on one instruction of the code
    - Type 1/2 Instruction modification without / with change of control flow
- Nature of error state can confirm to the nature of the originating fault
  - Transient vs. permanent, static vs. dynamic, single vs. multiple
  - Influence from utilized dependability means

## Hardware Error Models [Goloubeva]

- Mapping of hardware-level single bit-flip error to other layers
  - Memory data segment, processor data cache: System-level single data error
  - Memory code segment, processor code cache: System-level single code error of type 1 (modification of target register) or type 2 (modification of branch target)
  - Memory stack segment: System-level data error or type 2 code error
  - Processor register: Depending on processor architecture and register type
    - Single data error if register holds data interpreted by the application
    - Single type 1 code error, if register holds address used by load/store operation
    - Single type 2 code error, if register holds address of a branch target
  - Processor control register: Everything could happen ...

#### Hardware Error Models - Code Errors [Goloubeva]



Dependable Systems Course

# Software Error Models [Goloubeva]

- Similar terminology, but completely different semantics
- Syntactical errors are handled by compiler, semantical errors occur at runtime
  - Static vs. dynamic, permanent vs. temporary errors
- Example for C programming language
  - Errors affecting assignments (missing / wrong local variable values)
  - Errors affecting conditional instructions (wrong boolean or iteration condition)
  - Errors affecting function call / return (wrong parameters, return statement)
  - Errors affecting algorithms (missing statements or function calls, wrong operators)
- Under research in the software engineering field field studies, automated code analysis, developer interviews

# **Error Propagation**





#### Dependable Systems Course

# Error Propagation [Goloubeva]



# Error Message Occurrence (Hansen & Siewiorek)

- Same fault can lead to different (detected or undetected) errors
- Errors become detected by error detection mechanisms
  - Some undetected errors are detected by several detectors
  - Some detectors report several undetected errors together
  - Some undetected errors are not detected at all
- Detected errors might not be logged, if the system stops too fast



#### Failures

- Non-compliance with the specification arbitrary failure ('willkürlicher Ausfall')
- System failures can be further categorized in failure modes
  - Fail-silent / crash failure mode incorrect results are not delivered
  - Fail-stop mode constant value is delivered
- Failure mode view points
  - Failure mode **domain** what is influenced
    - Service result value failures, service timeliness timing failures
    - Service availability stopping failures
  - User perception in this mode consistent / inconsistent for all users
  - Failure **consequences** in this mode allow ordering of failure modes

# Failure Severity (,Schweregrad des Ausfalls')

- Denotes consequences of failure
- Benign failures (,unkritische Ausfälle')
  - Failure costs and operational benefits are similar
  - Sometimes also umbrella term for failures only detected by inspection
  - A system with only such failures is fail-safe
- Catastrophic failures (,kritische Ausfälle')
  - Costs of failure consequences are much larger than service benefit
- Significant / serious failures Intermediate steps expressing reduced service
- Grading of failure consequences on overall system depends on application
  - Flying airplane Catastrophic stopping failure, Train Benign stopping failure
- Criticality Highest severity of possible failure modes in the system

Dependable Systems Course
# Criticality Levels Example: DO-178B Standard

- Software Considerations in Airborne Systems and Equipment Certification
  - Mature document, developed for more than 20 years
- Definition of severity of failure conditions for airplane, crew, and passengers
  - Catastrophic Loss of ability to continue safe flight and landing
  - Major Reduced airplane or crew capability to cope with operating conditions
    - Reduction in safety margins and functional capabilities
    - Higher workload or physical distress for the crew
  - *Minor* Not significantly reduced airplane safety, slight increase in workload
  - No effect Failure results in no loss of operational capabilities and no increase in crew workload

## Example: DO-178B Standard



#### **Probability of Failure Condition**

# Failure Types

- Duration of the failure
  - Permanent failures no possibility for repairing or replacement
  - Recoverable failures back in operation after a fault is recovered
  - Transient failures short duration, no major recovery action
- Effect of the failure
  - Functional failures system does not operate according to its specification
  - Performance failures performance or SLA specifications not met
- Scope of the failure
  - Partial failure only parts of the system become unavailable
  - Total failure all services go down

## Swiss Cheese Model (Prof. Reason)

- Origins in medical research
- Defenses, barriers, and safeguards might be penetrated by fault trajectory



## **Observations on Failures**

- Failures vs. Load
  - Typically positive correlation
    - Increasing load can lead to wear-out increasing failure rate
    - Higher load can show up failure causes
    - Detected faults lead to recovery activities load increases
  - Feedback effects possible
- Related faults (attributed to a common cause) can lead to **common-mode failures**

## Chain of Dependability Threats



SOURCES OF ERRORS

[from Siewiorek and Swarz]

# Security - Vulnerability Assessment [Johnston]

- Different dependability attribute targets might lead to different terminology
- Example: Vulnerability assessment for nuclear security
  - **Threat**: Who might attack against what asset, using what resources, with what goal in mind, when / where / why, with what probability
  - Threat assessment (TA): Attempting to predict the threats proactive security
  - Vulnerability: Specific weakness in security that could be exploited
  - Vulnerability assessment (VA): Attempting to discover / demonstrate them
  - Risk management: Deploy, modify, and re-assign security resources, based on TA results, VA results, assets, security breach consequences, and costs (time, money, human resources)
  - Attack: Attempt to harm valuable asset by exploiting one or more vulnerabilities

## Security - Vulnerability Assessment [Johnston]

- Threats and vulnerabilities are different concepts, and must be treated separately
  - Vulnerabilities without threats are not interesting
  - Vulnerabilities do not define threats (bad locks do not imply thieves to show up)
- No one-to-one mapping, different attacks can exploit the same vulnerability
- TA involves mostly speculation about unknown people, so VA is more important
- Correct VA should identify large amount of issues with cheap countermeasures
- System features can become a vulnerability only in combination with an attack
- TA and VA are not pass / fail certifications

### Means for Dependability

- Fault prevention Prevent fault occurrence or introduction
- Fault tolerance Provide service matching the specification under faults
- Fault removal How to reduce the presence of faults
- Fault forecasting- Estimate the present number, future incidence, and the consequences of faults
- Combined utilization



## Dependability Means (Laprie)

- Offline / online techniques
  - Fault intolerance techniques
    - Fault prevention Prevent fault occurrence or introduction
    - Fault removal Reduce the presence of faults
    - 100% fault-free servicing for the whole life time is not possible
  - Fault tolerance techniques
    - Fault forecasting Estimate the present number, future incidence, and the consequences of faults
    - Fault tolerance Provide service complying with specification in spite of faults
- Problems with coverage and validation of the validator

## Dependable System Design (Echtle)



## Fault Prevention

- Specific approaches for avoiding faults
  - Specialized specification formalisms and techniques
  - Specialized development / manufacturing process to prevent design faults
  - Shielding
  - Only use ultra-reliable components
- General engineering approaches
  - Software engineering procedures
  - Quality management regulations and enforcement
  - Training and organization of maintenance departments

## Fault Removal

- Make faults disappear before fault tolerance becomes relevant
- Step 1: Verification
  - Check if the system adheres to **verification conditions**; if not, take next steps
  - Static verification: Static analysis, data flow analysis, compiler checks
  - Dynamic verification: Symbolic execution or verification testing
- Step 2: Diagnosis
  - Find the faults that influenced the verification conditions
- Step 3: Correction
  - Fix the problem, repeat the steps (**regression**)
- Fault removal during operation: Corrective maintenance (curative / preventive)

## Testing

- Selecting test inputs is driven from different view points
  - Testing purpose: conformance testing, fault-finding testing
  - System model: functional testing (with functional model) or structural testing
  - Fault model: enables fault-based testing
- Deterministic testing vs. random testing
- Structural testing of hardware is fault-finding, fault-based, structural testing
- Structural testing of software is fault-finding, non-fault-based, structural testing
- Golden unit: Reference system for comparison of output for a given input

# Fault Tolerance

• Fault tolerance is the ability of a system to operate correctly in presence of faults.

or

A system S is called k-fault-tolerant with respect to a set of algorithms {A<sub>1</sub>, A<sub>2</sub>, ..., A<sub>p</sub>} and a set of faults {F<sub>1</sub>, F<sub>2</sub>, ..., F<sub>p</sub>} if for every k-fault F in S, A<sub>i</sub> is executable by a subsystem of system S with k faults. (Hayes, 9/76)

or

- Fault tolerance is the use of **redundancy** (time or space) to achieve the desired level of system dependability costs !
- Accepts that an implemented system will not be fault-free
- Implements automatic recovery from errors
- Is a recursive concept (voter replication, self-checking checkers, stable memory)

## Fault Tolerance

- Typical design methodology in many technical and biological systems
  - Spare wheel in cars, redundant organs, ...
- Fault tolerance mechanisms need to be evaluated by dependability attributes
  - Minimum, maximum, average reliability and availability
  - Easy to formulate and understand, hard to prove failure rate remains unknown
  - Quantitative limits based on fault model (which faults in which components)
- Typically ,one-fault-at-a-time' assumption
- Different attributes of fault tolerance implementation to be checked
  - Functional verification, sensitivity analysis, minimum amount of resource resp. computational overhead, implementation performance, transparency, portability

### Phases of Fault Tolerance (Hanmer)



# Decomposition of Fault Tolerance (Lee & Anderson)

#### • Error detection

- Presence of fault is deducted by detecting an error in some subsystem
- Implies failure of the according component

#### Damage confinement

- Delimit damage caused due to the component failure
- Error processing recovery / compensation
  - System recovers from the effect of an error

#### • Fault treatment

• Ensure that fault does not cause again failures

## Fault Tolerance - Error Detection

#### Replication check

- Output of replicated components is compared / voted
- Independent failures, physical causes -> many replicas possible (e.g. HW)
- Finds also design faults, if replicated components are from different vendors
- Timing checks (,watchdog timers')
  - Timing violation often implies that component output is also incorrect
  - Typical solution for node failure detection in a distributed system
- Reasonableness checks Run-time range checks, assertions
- Structural and coding checks, diagnostics checks, algorithmic checks
- Ideal: Self-checking component with clear error confinement areas

## Fault Tolerance - Error Detection

- Replication checks are powerful and expensive, examples:
  - Execute identical copies on different hardware (component failures)
  - Execute separate and different versions (assumes independent design faults)
  - Execute same copies different times (transient faults)
  - Replicate only portion of the system
  - Works for both hardware and software
- Signaling aspect in the error detection task
  - Typical software model are exceptions, a way for implementing forward recovery
- Combination fault detection and fault location

# Fault Tolerance - Damage Confinement (Taylor)

#### System decomposition

- Every communication link might enable damage spreading
- Introduce mutual suspicion
- Hardware-based separation of software components
- OS-based separation (processes, runtime monitors, special shells)

#### Law-governed architecture

• Externalize contrains on interaction by runtime rules

#### Strongly-typed language

• Language guarantees the absence of unintended control flows

## Preventing Error Propagation

- Especially relevant when single components communicate their data
  - Single-source information local clock, sensor data, transaction status ...
  - Non-failed component must find an **agreement** how to treat received information
    - Special topic in distributed systems
    - Atomic broadcast, clock synchronization, membership protocols

# Fault Tolerance - Error Processing Through Recovery

#### • Forward error recovery

- Error is masked to reach again a consistent state (fault compensation)
- Corrective actions need detailled knowledge (damage assessment)
- New state is typically computed in another way
  - Examples: error correcting codes, non-journaling file system check, advanced exception handlers, (voters)

#### • Backward error recovery

- Roll back to previous consistent state (recovery point / checkpoint)
- Very suitable for transient faults
- Computation can be re-done with same components (retry), with alternate components (reconfigure), or can be ignored (skip frame)

## Fault Tolerance - Fault Treatment

- Fault diagnosis determine error cause's location and nature
- Fault passivation (remove faulty component &) reconfigure system
  - Error processing might already remove the fault , soft fault'
  - Typical example are temporary faults
- Fault tolerance manager
  - Careful diagnosis with hardware support
  - Damage assessment by disabling faulty components automatically
  - Example: IBM mainframe architecture
- Software rejuvenation
  - Gracefully terminating an application and immediately restarting it at a clean internal state

## Fault Tolerant Mindset (Hanmer)

- What can go wrong in any given situation ?
  - Mindset to be applied in all development stages
- "Every problem in computer science boils down to tradeoffs" [Henschen]
  - Fault prevention vs. fault tolerance vs. failure severity
- KISS principles, leave out "bells and whistles"
- Incremental additions of reliability long-term products
- Defensive Programming
  - Simple error handling; fix root cause, not symptoms; make data auditble; make code maintainable;

## Fault Tolerant Design Methodology (Hanmer)

- Assess things that can go wrong with the system (e.g. fault trees).
  - Find potential risks and according system failures.
- Define strategies to mitigate the identified risks.
  - Failure avoidance options, prevent faults from activation
- Create a mental model of the system design with redundancy.
- Design error detection and error processing capabilities.
- Design in the failure mitigation capabilities.
- Design human-computer interactions and modes of management.

## Dependable Design Strategies (Malek)

- Decompose the system
  - Identify fault classes, fault latency and fault impact for the components
  - Identify "weak spots" and assess potential damage
  - Integrate partial recovery / reintegration / restart
- Determine qualitative and quantitative specs for fault tolerance and evaluate your design in specific environment
- Develop / utilize fault and error detection techniques and algorithms
- Develop / utilize fault isolation techniques and algorithms
- Refine fault tolerance, iterate for improvement
- Re-use proven components, but be aware of integration issues

## Attributes of Dependability

- Non-functional attributes such as reliability and maintainability
- Complementary nature of viewpoints in the area of dependability
- In comparison to functional properties
  - ... hard to define
  - ... hard to abstract
  - $\bullet \dots$  ,Divide and conquer' does not work as good
  - ... difficult interrelationships
  - ... often probabilistic dependencies

![](_page_63_Figure_9.jpeg)

# Attributes of Dependability

- Reliability (,Funktionsfähigkeit') Continuity of service
  - Initial goal for computer system trustworthiness; other disciplines have different understanding
  - "Reliability is not doing the wrong thing." [Gray85]
  - "Reliability: Ability of a system or component to perform its required functions under stated conditions for a specified period of time" [IEEE]
  - "Reliability is the probability that an item will not fail." [Misra]
- Availability (,Verfügbarkeit') Readiness for usage
  - "Probability that a system is able to deliver correctly its service at any given time." [Goloubeva]
  - "Maintainability is the probability that the item can be successfully restored to operation after failure; and availability ... is a function of reliability and maintainability ." [Misra]

## Observations on Dependability Attributes

- Availability is always required
- Reliability, safety, and security may be optional
- Reliability might be analyzed for hardware / software components
- Availability is always from the system view point

## Attributes of Dependability

- Safety Avoidance of catastrophic consequences on the environment
  - Critical applications
  - Specification needs to describe things that should not happen
- Security Prevention of unauthorized access and / or information handling
  - Became especially relevant with distributed systems
- Confidentiality Absence of unauthorized disclosure of information
- Integrity Absence of improper system alteration
  - With respect to either accidental or intentional faults
- Maintainability Ability to undergo modifications and repairs

![](_page_66_Figure_10.jpeg)

## In Detail

### • Reliability - Function R(t)

- Probability that a system is functioning properly and constantly over time period t
  - Assumes that system was fully operational at t=0
  - Denotes failure-free interval of operation
- Availability Fraction of / points in time were a system is operational
  - Describe system behavior in presence of error treatment mechanisms (fault tolerance, repairing)
  - Instantaneous availability (at t) Probability that a system is performing correctly at time t; equal to reliability for non-repairable systems:  $A_i(t) = R(t)$
  - **Steady-state availability** Probability that a system will be operational at any random point of time, expressed as the fraction of time a system is operational during its expected lifetime:  $A_s(t) = Uptime / Lifetime$

# Reliability Definition: PDF & CDF

- Probability density function *pdf* for random variable *X* 
  - Discrete variable: Probability that X will be x
  - Continuous variable: Probability that X is in [a, b]
    - Computed as area under the density function in this range

$$P(a \le X \le b) = \int_{a}^{b} f(x) dx \text{ and } f(x) \ge 0 \text{ for all } x$$

 Cumulative distribution function *cdf(x)*: Probability that the value of X is at most x

$$F(x)=P(X\leq x)=\int_{0,-\infty}^x f(s)ds$$

- Limits of integration depend on the nature of the distribution function
- Value of *cdf* at *x* is always area under *pdf* up to *x*

![](_page_68_Figure_10.jpeg)

## **PDF** Examples

- Well-known statistical distributions, each describing a random variable behavior
- Parameters of the distribution derived from data, complete description then by *pdf*

70

![](_page_69_Figure_3.jpeg)

Normal distribution

![](_page_69_Figure_4.jpeg)

Probability density function

Cumulative distribution function

Dependable Systems Course

# The Reliability Function R(t)

- Reliability: Probability *R(t)* that a component works for time period [0,*t*]
- Idea: Express time period of correct operation as continuos random variable X
  -> time to failure
  - cdf(t) of this variable: Describes probability of failure before t -> Unreliability Function F(t)
  - 1-cdf(t): Describes probability of a failure after t -> time to failure -> Reliability Function R(t)
    - This works because working / non-working is a binary decision
- Typically, failures are modeled as Poisson process
  - Poisson properties lead to exponential distribution for the time between events
  - This time therefore only depends on failure rate parameter

![](_page_70_Figure_9.jpeg)

Dependable Systems Course

### Failure Rate

- Treat pdf for time-to-failure random variable X as failure density function
  - Can be computed as derivative of the unreliability function

f(t) = dF(t)/dt

- Failure rate / hazard rate function mean frequency of failures at time t
  - Conditional probability of a failure between a and b, given the survival until t

$$\lambda(t) = \frac{f(t)}{R(t)} = \lambda$$
 for constant failure rate
# Why Exponential ?

- Distribution function that models (beside others) the memoryless property of the Poisson process
  - P(T > t + s|T > t) = P(T > s), e.g.  $P_{Failure}(5 \text{ years}|T > 2 \text{ years}) = P_{Failure}(3 \text{ years})$
  - Failure is not the result of wear-out
  - Models ,intrinsic failure' part of the bath-tube curve, were most components spend the majority of their life time
  - Weibull distribution can also model tear-in and wear-out
- Some natural phenomena have constant failure rate (e.g. cosmic ray particles)
- Example: Product support determines an outage rate of 0.5% per day, independent from age
  - Failure rate is 0.005, so mean time to failure = 200 days
  - Numerical formulation for "law of small numbers"

Dependable Systems Course

g

## The Reliability Function R(t)

- Failures occur continuously and independently at a constant average rate (Poisson process)
- Increasing probability of failure with increasing t - cdt function
- Failure rate  $\lambda$  from experience or complexity measures
- Cumulative distribution function:

 $F(x;\lambda) = \begin{cases} 1 - e^{-\lambda x}, & x \ge 0, \\ 0, & x < 0. \end{cases}$ 



Reliability function (survival probability) for exponential failure distribution:

$$R(t) = P(X > t) = 1 - F(t) = e^{-\lambda x}$$
 with  $F(x) = 1 - e^{-\lambda x}$ 

### Variable Failure Rate in Real World



- Failure rate is treated as constant parameter of the exponential distribution
- (maybe invalid) simplification, mostly combined solution in practice:
  - Exponential distribution when failure rate is constant
  - Weibull distribution when failure rate is monotonic decreasing / increasing

#### Hardware Failure Rate



### Software Failure Rate

Industrial practice

• When do you stop testing ? - No more time, or no more money ...



(C) Malek

#### Failure Rate Examples

- Standards from experience provide base data for component reliability
- Society of Automotive Engineers (SAE) reliability model

$$\lambda_p = \lambda_b \Pi_{i=1}^b \pi_i$$

- ullet Predicted failure rate  $\,\lambda_p$
- Base failure rate for the component  $\lambda_b$
- ullet Various modification factors  $\,\pi_i$ 
  - Component composition
  - Ambient temperature
  - Location in the vehicle

## Example: Item-Level Sparing Analysis [Misra]

- Sparing analysis challenges
  - How many spares do you need to keep the system available at the desired rate ?
  - When are you going to need to spares (manufacturing time) ?
  - Where the spares should be kept?
  - What system level you want to spare at ?

### Steady-State Availability

- Mean time to failure (MTTF) -Average time it takes to fail
- Mean time to recover / repair (MTTR) Average time it takes to recover
- Mean time between failures (MTBF) -Average time between two successive failures





## Steady-State Availability and MTBF

- Expressing reliability with MTBF ,should' imply a repairable system
  - If all failures can be repaired, the MTBF estimate can become constant as time tends to infinity
  - In reliable systems, the downtime is short in comparison to uptime, so the steady-state condition holds earlier
  - MTBF = MTTF + MTTR
  - Availability = MTTF (accumulated up time) / MTBF (accumulated life time) = MTTF / (MTTF + MTTR)
- Expressing reliability with MTTF ,should' imply a non-repairable system
  - MTBF (mean time BEFORE failure) = MTTF -> typical source of confusion
- If time to failure is exponentially distributed, then the reciprocal of the rate parameter is equivalent to the distribution mean

$$\lambda = \frac{1}{MTTF}$$

#### Example

- Test population with 50 HDDs and 100 hours of testing, 2 drives fail during the test
  - As usual, we assume exponential distribution of the time to failure
  - Reliability at t=100 is known to be 98%
  - Reciprocal of the according failure rate is the MTTF

$$R(t) = P(X > t) = 1 - F(t) = e^{-\lambda x} \text{ with } F(x) = 1 - e^{-\lambda x}$$
$$R(100hours) = e^{-\lambda 100} = 0.98$$
$$\lambda = -\frac{\ln 0.98}{100} = 0,000202$$
$$MTTF = \frac{1}{\lambda} = 4949,831hours$$

### MTBF / MTTF in Practice

- Often express average failure behavior (statistics) for a component population
- Good for relative comparison, not for expected life time expectation of one unit
- Example: Hard disk with MTTF of 500.000 hours and 5 years of expected operation (,service life')
  - Drive of this type is expected to run 5 years without problems
  - Large group of such drives will (on average) have one failed drive after 500.000 hours of **accumulated** life time
  - What to buy: Model with longer MTBF or longer warranty time ?

## **Operational Availability Calculation [Misra]**

- Uptime elements: Standby time, operating time
- **Downtime** elements
  - Logistic: Spares availability, spares location, transportation of spares
  - Preventive maintenance: Inspection, servicing
  - Administrative delay
    - Finding personnel, reviewing manuals, complying with supply procedures, locating tools, setting up test equipment
  - Corrective maintenance
    - Preparation time, fault location diagnosis, getting parts, correcting faults, testing

## MTTR Examples

- Hardware MTTR with spares onsite
  - Operator available 30min
  - Operator on call 2 hours
  - Operator available during working hours 14h
  - Without spares at least 24h
- SW MTTR with watchdog
  - Reboot from ROM 30s
  - Reboot from disk 3 min
  - Reboot from network 10 min

## Steady-State Availability

$$A = \frac{Uptime}{Uptime + Downtime} = \frac{MTTF}{MTTF + MTTR}$$

Availability	Downtime per year	Downtime per week
90.0 % (1 nine)	36.5 days	16.8 hours
99.0 % (2 nines)	3.65 days	1.68 hours
99.9 % (3 nines)	8.76 hours	10.1 min
99.99 % (4 nines)	52.6 min	1.01 min
99.999 % (5 nines)	5.26 min	6.05 s
99.9999 % (6 nines)	31.5 s	0.605 s
99.99999 % (7 nines)	0.3 s	6 ms

## MTTR >> MTTF [Fox]

- Armando Fox on ,Recovery-Oriented Computing'
  - A = MTTF / (MTTF + MTTR)
    - 10x decrease of MTTR as good as 10x increase of MTTF ?
    - MTTF's are not claimable, but MTTR claims are verifiable
    - Proving MTTF numbers demands system-years of observation and experience
    - Lowering MTTR directly improves user experience of one specific outage, since MTTF is typically longer than one user session
  - HCI factor of failed system
    - Miller, 1968: >1sec "sluggish", >10sec "distracted" (user moves away)
    - 2001 Web user study: ~5sec "acceptable", ~10sec "excessively slow"

## MTTR >> MTTF [Fox]

- Proposal: Utility curve for recovery time
  - Factors: Length of recovery time, level of service availability during error state
  - Key distinction between interactive (session-based) and non-interactive systems
- If error state leads to some steady-state latency
  - For how long will users tolerate temporary degradation ?
  - How much degradation is acceptable ?
  - Do they show a preference for increased latency vs. worse QOS vs. being turned away and incentivized to return?
- Long recovery times are often reasoned by stateful components
  - Utilize alternative architecture concepts

## Availability

